

1 次の不等式を解け。

- (1) $(x+2)(x-3) < 0$ (2) $x(3x-1) > 0$ (3) $(2x+3)(3x-4) \leq 0$
 (4) $x^2-4 < 0$ (5) $x^2-3x+2 > 0$ (6) $2x^2+9x+9 \geq 0$
 (7) $-3x^2+10x-8 > 0$ (8) $3x^2-\sqrt{7}x-1 \geq 0$ (9) $x^2+x \leq 3x+24$
 (10) $3x^2-7x+2 < 0$ (11) $2x^2-7x-4 \leq 0$ (12) $6x^2-7x-3 > 0$
 (13) $x^2-4x+2 > 0$ (14) $x^2+5x+1 < 0$ (15) $2x^2+5x-1 \geq 0$
 (16) $x^2 < 4$ (17) $x^2-18 > 0$ (18) $2x^2-9 \geq 0$

- 解答 (1) $-2 < x < 3$ (2) $x < 0, \frac{1}{3} < x$ (3) $-\frac{3}{2} \leq x \leq \frac{4}{3}$ (4) $-2 < x < 2$
 (5) $x < 1, 2 < x$ (6) $x \leq -3, -\frac{3}{2} \leq x$ (7) $\frac{4}{3} < x < 2$
 (8) $x \leq \frac{\sqrt{7}-\sqrt{19}}{6}, \frac{\sqrt{7}+\sqrt{19}}{6} \leq x$ (9) $-4 \leq x \leq 6$
 (10) $\frac{1}{3} < x < 2$ (11) $-\frac{1}{2} \leq x \leq 4$ (12) $x < -\frac{1}{3}, \frac{3}{2} < x$
 (13) $x < 2-\sqrt{2}, 2+\sqrt{2} < x$ (14) $\frac{-5-\sqrt{21}}{2} < x < \frac{-5+\sqrt{21}}{2}$
 (15) $x \leq \frac{-5-\sqrt{33}}{4}, \frac{-5+\sqrt{33}}{4} \leq x$ (16) $-2 < x < 2$
 (17) $x < -3\sqrt{2}, 3\sqrt{2} < x$ (18) $x \leq -\frac{3\sqrt{2}}{2}, \frac{3\sqrt{2}}{2} \leq x$

2 次の2次不等式を解け。

- (1) $(x-3)(x-5) < 0$ (2) $(x-2)(x+7) > 0$ (3) $x(x+4) \geq 0$
 (4) $(2x-3)(3x+1) \leq 0$ (5) $x^2-5x-6 \geq 0$ (6) $x^2+11x+18 < 0$
 (7) $x^2+12 \geq 7x$ (8) $x^2-8x \leq 0$ (9) $x^2 \geq 25$
 (10) $2x^2-5x-3 \leq 0$ (11) $6x^2+x-2 > 0$ (12) $x^2-4x+2 \geq 0$
 (13) $x^2+5x+1 < 0$ (14) $2x^2-9 > 0$ (15) $-3x^2+6x-2 \geq 0$
 (16) $-x^2+3x+10 < 0$ (17) $3x-x^2 \geq 0$ (18) $-3x^2+6x-2 \geq 0$

- 解答 (1) $3 < x < 5$ (2) $x < -7, 2 < x$ (3) $x \leq -4, 0 \leq x$
 (4) $-\frac{1}{3} \leq x \leq \frac{3}{2}$ (5) $x \leq -1, 6 \leq x$ (6) $-9 < x < -2$
 (7) $x \leq 3, 4 \leq x$ (8) $0 \leq x \leq 8$ (9) $x \leq -5, 5 \leq x$
 (10) $-\frac{1}{2} \leq x \leq 3$ (11) $x < -\frac{2}{3}, \frac{1}{2} < x$ (12) $x \leq 2-\sqrt{2}, 2+\sqrt{2} \leq x$
 (13) $\frac{-5-\sqrt{21}}{2} < x < \frac{-5+\sqrt{21}}{2}$ (14) $x < -\frac{3\sqrt{2}}{2}, \frac{3\sqrt{2}}{2} < x$
 (15) $\frac{3-\sqrt{3}}{3} \leq x \leq \frac{3+\sqrt{3}}{3}$ (16) $x < -2, 5 < x$ (17) $0 \leq x \leq 3$
 (18) $\frac{3-\sqrt{3}}{3} \leq x \leq \frac{3+\sqrt{3}}{3}$

3 次の不等式を解け。

- (1) $(x-4)^2 > 0$ (2) $(x-4)^2 \geq 0$ (3) $(x-4)^2 < 0$
 (4) $(x-4)^2 \leq 0$ (5) $x^2-8x+16 < 0$ (6) $9x^2+1 \leq 6x$
 (7) $(x-3)^2+2 > 0$ (8) $x^2-2x+5 \leq 0$ (9) $x^2 < -2-2x$
 (10) $x^2+7x+6 \leq 0$ (11) $x^2-2x-15 > 0$ (12) $2x^2+x-6 < 0$
 (13) $-x^2+2x+4 \leq 0$ (14) $x^2-12x+36 > 0$ (15) $9x^2+24x+16 \leq 0$
 (16) $x^2-x+3 \geq 0$ (17) $-2x^2-6x-5 > 0$

- 解答 (1) $x=4$ 以外のすべての実数 (2) すべての実数 (3) 解はない
 (4) $x=4$ (5) 解はない (6) $x=\frac{1}{3}$ (7) すべての実数 (8) 解はない
 (9) 解はない (10) $-6 \leq x \leq -1$ (11) $x < -3, 5 < x$ (12) $-2 < x < \frac{3}{2}$
 (13) $x \leq 1-\sqrt{5}, 1+\sqrt{5} \leq x$ (14) 6 以外のすべての実数 (15) $x = -\frac{4}{3}$
 (16) すべての実数 (17) 解はない